I. Moment-tensor analysis using global data

- 2. The Harvard (= Global) CMT catalog
- 3. Using calibration information in waveform analysis
- 4. Data quality control using noise
- 5. Data quality control using signals
- 6. Finding interesting things in the noise

# Faulting force model



The elastic stress release in an earthquake is described by a double couple of forces

### The nine dipoles of the seismic moment tensor



But, Mxy=Myx, Myz=Mzy, Mxz=Mzx



for example,  $10^{28}$  dyne-cm =  $10^{24}$  dyne x 10000 cm





The vibrations caused by a force acting on or in the Earth can be modeled by summation of Earth's normal modes



$$u(\boldsymbol{x},t) = \sum_{k} \left[1 - \exp\left[-\alpha_{k}(t-t_{s})\right] \cos \omega_{k}(t-t_{s})\right] \boldsymbol{f} \cdot \boldsymbol{w}^{(k)}(\boldsymbol{x}_{s}) \boldsymbol{s}_{k}(\boldsymbol{x})$$

where f is the force vector and  $w^k$  is the displacement of the k-*th* mode.

#### Moment-tensor analysis by waveform fitting

(Observed seismogram)/(Instrument response) x Filter = Observed waveform (Synthetic displacement seismogram) x Filter = Model waveform

Model waveform depends on:

Earthquake parameters
Earth structure

If the Earth structure and the earthquake location are known, the Model waveform depends only on the six elements of the moment tensor,  $M_{xx}$ ,  $M_{yy}$ ,  $M_{zz}$ ,  $M_{xy}$ ,  $M_{xz}$ , and  $M_{yz}$ 

Minimize the difference [Observed waveform - Model waveform]<sup>2</sup> with respect to the moment tensor elements.

#### Detection and analysis of large earthquakes: GLOBAL SEISMOGRAPHIC NETWORK



Current GSN station coverage of Earth is shown as of August 2005. Sites added in the past five years are noted in purple (stations) and orange (arrays). Sites planned to be completed are noted with white stars. Cooperative sites are indicated by symbols on the upper right "shoulder" of the stars.





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Minimize the difference [Observed waveform - Model waveform]<sup>2</sup> with respect to the moment tensor elements.

#### **Seismogram Modeling**

The k-*th* seismogram in a data set for a given earthquake can be represented by:

$$u_k(\mathbf{r},t) = \sum_{i=1}^N \psi_{ik}(\mathbf{r}_0,\mathbf{r},t)f_i$$

where  $\psi_{ik}$  are the excitation kernels and  $f_i$  are independent parameters of the source model.

 $f_1 = Mzz, f_2 = Myy, etc.; N=6$ 

# Seismogram Synthesis for a Moment-Tensor Source

The seismic displacement field can be calculated by superposition of the normal modes of the Earth (Gilbert, 1971):

$$u(\boldsymbol{x},t) = \sum_{k} \left[1 - \exp\left[-lpha_{k}(t-t_{s})\right] \cos \omega_{k}(t-t_{s})\right] \boldsymbol{M}$$
 :  $e^{(k)}(\boldsymbol{x}_{s}) \boldsymbol{s}_{k}(\boldsymbol{x})$ 

where  $\alpha_k$  is the decay constant of and  $e^k$  is the strain tensor in the k-th mode;  $s_k$  is the eigenfunction of the k-th mode; and M is the seismic moment tensor.



# Fit to seismograms: Body waves at Eskdalemuir, Scotland



blue - data ; red - model

## Fit to seismograms: Surface waves at Hockley, Texas



blue - data ; red - model

#### **Estimation of the Source Parameters**

For a point source, the elements  $f_i$  can be estimated by solving  $\mathbf{A} \cdot \mathbf{f} = \mathbf{b}$ , where:

$$A_{ij} = \sum_{k} \int_{t_{k_1}}^{t_{k_2}} \psi_{ik} \psi_{jk} dt \; ; \; b_j = \sum_{k} \int_{t_{k_1}}^{t_{k_2}} u_k \psi_{jk} dt.$$

This procedure requires that the position of the source  $(r_0, t_0)$  be known.

#### Solution for the Source Centroid

The earthquake centroid can be determined simultaneously with the source model parameters by expansion of the equations of condition to allow for a perturbation in the location of the source (Dziewonski, Chou and Woodhouse, 1981):

$$u_k = u_k^{(0)} + \{\psi_{ki,j}^{(0)} \cdot \delta x_j - \psi_{ki,t}^{(0)} \cdot \delta t_0\} \cdot f_i^{(0)} + \psi_{ki}^{(0)} \cdot \delta f_i;$$

where the superscript (0) indicates parameters determined for the starting location. The problem can then be solved iteratively.

# Iterative procedure for moment-tensor source converges nicely



# One week of quick CMTs



# 2. The Harvard (= Global) CMT catalog

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The Harvard / Global CMT Project

Project started in 1981 (A.M. Dziewonski et al.)

Goal is (now) to determine source parameters for all earthquakes with M>5 worldwide

CMT catalog contains ~25,000 moment tensors for the period 1976-2006

In 2006 the project moved from Harvard University to Lamont/Columbia University

#### Shallow earthquakes, 1976-2006 (approximately 3000) 30N õ 15N **D**ON 15S 30S 8 45S 0 0S 90W 120W 105W 75W 60W 45W ЗÕ





# The CMT catalog can be accessed now at <u>www.seismology.harvard.edu</u>

and soon at <u>www.globalcmt.org</u>

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# HLGP seismometer and recording system



Original calibration pulses and pulses for nominal response



Original calibration pulses and pulses for new response after inversion

Comparison of waveforms after normalizing responses for two stations in the same location





Some channels were reversed for some periods of time



Some channels had extra filters for some periods of time

(Ekström and Nettles, PEPI, 1997)

Waveform comparisons (observed and synthetic) after correcting seismograms using new responses: The 1976 Friuli earthquake

> Main Shock 6 May 1976

> > A&J

Aftershock

Friuli Events

C80

C80

СМТ

СМТ



4. Data quality control using noise

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# Noise spectra from the Global Seismic Network











5. Data quality control using signals

6. Finding interesting things in the noise

## Blue - observed seismograms Red - synthetic seismograms



### Blue - observed seismograms Red - synthetic seismograms



















#### Stations for which a time- and frequency-dependent change in response is observed

Station	Network	Component	Start <sup>a</sup>	$\operatorname{End}^b$	Comment
ABKT	II	LHZ	1995	1997	
BJT	IC	LHZ	1999	2004	
BRVK	II	LHZ	2001	2004	
CMB	BK	LHE	1996	2000	Seismometer replaced in 2000
HRV	IU	LHE	1996	2004	
HRV	IU	LHN	1990	2004	
KCC	BK	LHZ	1999	2004	
KCC	BK	LHN	2000	2004	
KCC	BK	LHE	2002	2004	
KEG	MN	LHZ	1995	1998	No scaling data after 1998
KIP	IU	LHZ	2004	2004	Only one year with anomalous scaling
LVZ	II	LHZ	1995	2004	
MA2	IU	LHE	1998	2004	
PAB	IU	LHE	1999	2004	
PEL	G	LHZ	1999	2001	No scaling data after 2001
PEL	G	LHN	1999	2003	No scaling data after 2003
PEL	G	LHE	1998	2001	No scaling data after 2001
PET	IU	LHN	2002	2004	
SAO	BK	LHZ	2001	2004	
SSE	IC	LHN	2000	2004	
SSB	G	LHZ	2002	2004	

<sup>a</sup>Year in which the change in response is first clearly observed

<sup>b</sup>Year in which the change is last observed (2004 is the most recent year analyzed)

(Ekström, Dalton, and Nettles, SRL, 2006)

# Summary

- All results are available at: <u>www.seismology.harvard.edu/</u> <u>~ekstrom/Projects/WQC/SCALING</u>
- Most stations show no, or small, deviations from the reported response
- A few stations (e.g., GTSN) show constant offsets in gain of 10-20%
- Approximately 15% of stations equipped with STS-1 seismometers show a time- and frequency-dependent deterioration of the true gain
- Cause of problem?
  - How to fix instruments?
  - How to fix response information retroactively?
- Recommend regular instrument calibration

6. Finding interesting things in the noise

Seismographs record signals with frequencies between ~10 Hz to 1000 seconds.

Earthquakes are detected and located using high-frequency signals (around 1 Hz).

Are there short-lived geophysical phenomena that generate seismic waves at long periods but that are not detected at short periods?



#### **Surface-wave dispersion**

Seismic surface waves are dispersive,  $c = c(\omega)$ , where  $\omega = \frac{2\pi}{T}$  and T is the period of the waves.

Travel time  $\tau$  is therefore dependent on frequency,  $\tau(\omega)$ .

Propagation phase  $\Phi(\omega) = \omega \cdot \tau(\omega) = \frac{\tau(\omega) \cdot 2\pi}{T}$ .

For the propagation phase from point  $(\theta_A, \varphi_A)$  to point  $(\theta_B, \varphi_B)$  we write,

$$\Phi(\omega) = \int_{A}^{B} \frac{\omega}{c(\theta,\varphi;\omega)} ds$$

with velocity depending on position,  $c(\theta, \varphi)$ .







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## 1. Collect seismograms from the GSN

## 2. Low-pass filter, 35-250 s period







4. Calculate dispersion curves to all stations

- 5. Deconvolve propagation effects from all seismograms
- 6. Calculate envelope function









# 1999 Alaska Range earthquake detection

Approximate location of mystery event



# Comparison of seismograms














## Mechanism of melt water lubrication of glacial base



**Fig. 2.** Schematic of glaciological features in the equilibrium and ablation zones, including surface lakes, inflow channels, crevasses, and moulins. Ice flow for basal ice at the pressure melting point is partly from basal sliding and partly from shear deformation, which is mostly in a near-basal boundary layer.

from Zwally et al., Science, 2002

## Increasing frequency of Greenland glacial earthquakes





Howat et al., 2005; Hamilton & Stearns, 2005